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Measuring Progress in Learning

Accountability has the natural tendency to force people to prove themselves by providing measureable evidence. However, learning is not so easily measurable as it is personal and dependent on so many different things. It has been shown there is more variation within a single student than across a class of students.

True learning is something that is achieved over time and with effort on the part of the learner and the support and challenge from the teacher. But we are still required to measure progress.

There are 10 key findings for making a bigger difference in mathematics teaching (Derived from a range of national and international monitoring data and research including NEMP, TIMSS, PISA, ERO and 103 NDP evaluations & studies)

Key Finding number 6

Assessment for Learning:

Effective teachers make use of a wide range of formal and informal assessments to monitor learning progress, diagnose learning issues and determine what they need to do next to further learning. IN THE COURSE OF REGULAR CLASSROOM ACTIVITY they collect information about students learning. Moment by moment assessment of student progress helps decide what questions to ask, when to intervene and how to respond to questions. Teachers gain a lot by observing and listening. A TEACHER SHOULD NOT BE TALKING ALL THE TIME.

One on one interviews can also provide important insights. A thinking aloud problem solving interview will often reveal more about what is going on in a student's mind than a written test.

By asking questions, effective teachers require students to participate in mathematical thinking and problem solving. A key indicator of good questioning is how a teacher listens to student responses. Effective teachers pay attention not only to whether an answer is correct but also to the students' mathematical thinking. Teachers need to have an understanding of the thinking progressions as manifested in the mathematics being undertaken by the students. Progressions and frameworks strengthen teacher knowledge of student thinking.

Advice given on NZMaths under tracking progress and achievement:

Teachers are encouraged to plan opportunities to notice what their students can do in their regular teaching and learning programmes. This may involve identifying specific activities that provide a rich source of information about how students are going on key learning outcomes. By observing students as they work in class, asking probing questions, listening to explanations, and looking at students' workbooks, teachers can determine what students know and can do. They can use this information to improve the teaching and learning of mathematics and to make judgments about achievement. The most authentic assessment tasks are those that are included in the learning experiences of the students, rather than as stand alone tests.

In addition to noticing what students know and can do in teaching and learning programmes, there are a range of assessment tools available to collect particular information about students, **as required.**

Use an assessment tool only for specific students or for a specific reason that will be for the benefit of the students progress.

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What Assessment Tools are available for Mathematics

There is no ministry approved assessment tool (only ministry funded). It is up to schools and individual teachers to decide which tool is going to give them the extra information they require.

Assessment Tool	Year Groups	Assessment Type
Progressive Achievement Tests (PAT)	year 3+	Multi choice
e-asTTle	Year 5+	Multi choice
GloSS	year 3+	Individual Interview
JAM	Year 1 - 3	Individual Interview
Numeracy Baseline	Year 0 - 1	Evidence collected over period of time: Language and basic number knowledge
Primary Maths Assessment Tool (PMAT) (Level 1 sections 1 & 2)	Year 1 - 2	Individual Interview Early knowledge & simple problems
Primary Maths Assessment Tool (PMAT) (Upper Level 1 to Early Level 3 (sections 3 & 4)	Year 2 - 6+	Problem solving: Small group guided paper recording)
Primary Maths Assessment Tool (PMAT) (Level 3 - 4 sections 5 & 6)	Year 6 - 10	Problem solving: Individual recording & conferencing
Wilkie Way Assessment Screens Level 1 - 4	Year 3 - 10	Key knowledge and skills. Recorded

Numeracy Baseline available FREE at www.wilkieway.co.nz Maths News & Information Use the Assessment TAB or Foundation Years TAB to locate the downloadable file.

Primary Maths Assessment Tool (PMAT) available from edify.co.nz

Wilkie Way Assessment Screens available from the online store at wilkieway.co.nz

GIOSS & JAM available from NZMAths website Tracking Progress & Achievement/Assessment Tools

Progressive Achievement Tests (PAT) information available from NZCER website

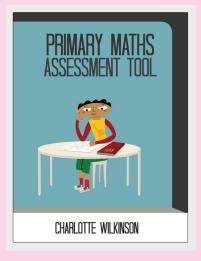
e-asTTIe - information available from TKI website



Pearson Mathematics & Maths Aotearoa have

mini projects designed to also be used as assessment tasks, with assessment criteria identified.

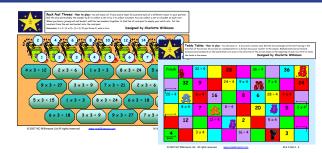
Maths Aotearoa also identifies the learning progression the mini project could provide evidence for. (Available from edify.co.nz)



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Resources for Wilkie Way Members Subscriptions purchased at the online store at www.wilkieway.co.nz Individual \$45 - paid via paypal NZ School paid via invoice - complete form at online store Up to 100 students \$150+GST 101 - 300 students \$250 + GST 300+ students \$350 +GST Non NZ School \$400 - paid via paypal

New Resources Numeracy Games: New Folder: Multiplication and Division Games 17 games have been added to this folder. Some of these games need 0 - 9 dice



Problems with Shopping can be downloaded as a single sheet from Graduated Problems on a Theme



May Featured Resources

Teacher Professional Resurces: Learning Progressions

This learning progression chart assists teachers to see how the progressions that unpack all the strands of the NZ curriculum (and sit behind the PACT tool) progress from level 1 to level 4 (read horizontally) and how they connect with each other. (Read vertically). An essential chart for implementing the curriculum.

	kie Way ir	iterpretation	of the le	earning progre	essions to	assist the n	noderation of	students work ag	gainst curriculum levels
	Leve	11		Level 2			Level 3		Level 4
Additive T									
Recognises 1,2,3 by subatizing	1 - 1 matching Makes a set up to 10. Subatizes patterns to 6	solves result and fingers	roblem Uses p to double ses on fact or place v	7- 10 from any number artitions to 10, Uses s, uses +/- patterns based to 10, knows standard ralue partitions decade numbers work like	addition and subtr Uses Rounding an	tition for double digit action. d compensating ary addition to solve 15.	Set 7 Estimates results of additi Uses equal addition or inwe find difference. Uses a standard algorithm Uses standard partitioning decimals	erse operations to integers, decin	ty with whole numbers, nais and fractions.
Multiplicat	tive Thinking								
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	nd Relationship								
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Using Syn	bols and Expres								
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Geometric				pressions		division.			
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For further unpacking progressions of learning there are progressions for:

- Addition & Subtraction
- Multiplication & Division
- Fractions
- Place Value
- Number Operations (Previous four combined) by curriculum level
- Geometric Progressions
- Measurement Progressions





Problems with Shopping

Tyler had \$10



He bought a drink and a doughnut and had no money left.

How much could each item have cost?

Sita went shopping and bought three items costing \$25, \$18 and \$43

How much did she spend altogether?

What is the difference in price between the most expensive and the cheapest item?



The shopping bill came to \$234



Only \$168 was for food. The rest was spent on a present for mum.

\$78.95

How much was the present?

Leila loves shopping.

She had saved \$250 to go on a shopping trip.

She wanted to buy 3 items costing \$48.50

\$105.75

Does she have enough money and if so how much change would she have?

